



5. $f(x + y) + f(x - y) = 2f(x) \cos y.$

Solution:

$$f(x) = C_1 \cos x + C_2 \sin x,$$

where C_1 and C_2 are arbitrary constants.

Reference

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