



First-Order Partial Differential Equations > Linear Equations > Section 1.1

3.
$$\frac{\partial w}{\partial x} + [f(x)e^{\lambda y} + g(x)] \frac{\partial w}{\partial y} = 0.$$

1°. Principal integral: $\Xi = e^{-\lambda y} E + \lambda \int f(x) E dx$, where $E = \exp \left[\lambda \int g(x) dx \right]$.

2°. General solution: $w = \Phi(\Xi)$, where $\Phi(\Xi)$ is an arbitrary function.

Reference

Polyanin, A. D., Zaitsev, V. F., and Moussiaux, A., *Handbook of First Order Partial Differential Equations*, Taylor & Francis, London, 2002.