



4.  $y(x) + \lambda \int_a^x (x-t)^3 y(t) dt = f(x).$

Solution:

$$y(x) = f(x) - \int_a^x R(x-t)f(t) dt,$$

where

$$R(x) = \begin{cases} k [\cosh(kx) \sin(kx) - \sinh(kx) \cos(kx)], & k = \left(\frac{3}{2}\lambda\right)^{1/4} \text{ for } \lambda > 0, \\ \frac{1}{2}s [\sin(sx) - \sinh(sx)], & s = (-6\lambda)^{1/4} \text{ for } \lambda < 0. \end{cases}$$

### Reference

**Polyanin, A. D. and Manzhirov, A. V.,** *Handbook of Integral Equations*, CRC Press, Boca Raton, 1998.