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$$2. \quad i \frac{\partial w}{\partial t} + \frac{\partial^2 w}{\partial x^2} + A|w|^{2n}w = 0.$$

Schrodinger (Schrödinger) equation with a power-law nonlinearity. Here, w is a complex functions of real variables x and t ; A and n are real numbers, $i^2 = -1$.

1°. Solutions:

$$w(x, t) = C_1 \exp\{i[C_2x + (A|C_1|^{2n} - C_2^2)t + C_3]\},$$

$$w(x, t) = \pm \left[\frac{(n+1)C_1^2}{A \cosh^2(C_1nx + C_2)} \right]^{\frac{1}{2n}} \exp[i(C_1^2t + C_3)],$$

$$w(x, t) = \frac{C_1}{\sqrt{t}} \exp \left[i \frac{(x + C_2)^2}{4t} + i \left(\frac{AC_1^{2n}}{1-n} t^{1-n} + C_3 \right) \right],$$

where C_1 , C_2 , and C_3 are arbitrary real constants.

2°. There is a self-similar solution of the form $w = t^{-1/(2n)}u(\xi)$, where $\xi = xt^{-1/2}$.

3°. For other exact solutions, see the [nonlinear Schrodinger equation of general form](#) with $f(u) = Au^{2n}$.

References

Ablowitz, M. J. and Segur, H., *Solitons and the Inverse Scattering Transform*, Society for Industrial and Applied Mathematics (SIAM), Philadelphia, 1981.

Akhmediev, N. N. and Ankiewicz, A., *Solitons. Nonlinear Pulses and Beams*, Chapman & Hall, London, 1997.

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