



1. $\frac{\partial^2 w}{\partial x^2} + \frac{\partial^2 w}{\partial y^2} = aw + bw^n.$

1°. Traveling-wave solutions for $a > 0$:

$$w(x, y) = \left[\frac{2b \sinh^2 z}{a(n+1)} \right]^{\frac{1}{1-n}}, \quad z = \frac{1}{2} \sqrt{a} (1-n)(x \sin C_1 + y \cos C_1) + C_2 \quad \text{if } b(n+1) > 0,$$

$$w(x, y) = \left[-\frac{2b \cosh^2 z}{a(n+1)} \right]^{\frac{1}{1-n}}, \quad z = \frac{1}{2} \sqrt{a} (1-n)(x \sin C_1 + y \cos C_1) + C_2 \quad \text{if } b(n+1) < 0,$$

where C_1 and C_2 are arbitrary constants.

2°. Traveling-wave solutions for $a < 0$ and $b(n+1) > 0$:

$$w(x, y) = \left[-\frac{2b \cos^2 z}{a(n+1)} \right]^{\frac{1}{1-n}}, \quad z = \frac{1}{2} \sqrt{|a|} (1-n)(x \sin C_1 + y \cos C_1) + C_2.$$

3°. For $a = 0$, there is a self-similar solution of the form $w = x^{\frac{2}{1-n}} F(z)$, where $z = y/x$.

4°. For other exact solutions of this equation, see equation 3.1.7 with $f(w) = aw + bw^n$.

Reference

Polyanin, A. D. and Zaitsev, V. F., *Handbook of Nonlinear Partial Differential Equations*, Chapman & Hall/CRC, Boca Raton, 2004.