



Exact Solutions > Ordinary Differential Equations > First-Order Ordinary Differential Equations > Riccati Equation, Special Case 1

11. $y'_x = f(x)y^2 + anx^{n-1} - a^2x^{2n}f(x).$

Riccati equation, special case 1.

Particular solution: $y_0 = ax^n.$

The general solution can be written as:

$$y = ax^n + \Phi(x) \left[C - \int f(x)\Phi(x) dx \right]^{-1}, \quad \text{where } \Phi(x) = \exp \left[2a \int x^n f(x) dx \right],$$

C is an arbitrary constant.

Reference

Polyanin, A. D. and Zaitsev, V. F., *Handbook of Exact Solutions for Ordinary Differential Equations, 2nd Edition*, Chapman & Hall/CRC, Boca Raton, 2003.

Riccati Equation, Special Case 5