



41. $x^2 y''_{xx} + x f y'_x + a(f - a - 1)y = 0, \quad f = f(x).$

Particular solution: $y_0 = x^{-a}.$

Solution:

$$y = y_0 \left(C_1 + C_2 \int \frac{e^{-F}}{y_0^2} dx \right), \quad \text{where } F = \int x^{-1} f dx,$$

C_1 and C_2 are arbitrary constants.

Reference

Polyanin, A. D. and Zaitsev, V. F., *Handbook of Exact Solutions for Ordinary Differential Equations, 2nd Edition,* Chapman & Hall/CRC, Boca Raton, 2003.