



$$8. \quad \frac{\partial^2 u}{\partial t^2} = \frac{a}{x^n} \frac{\partial}{\partial x} \left(x^n \frac{\partial u}{\partial x} \right) + u f(u^2 - w^2) + w g(u^2 - w^2),$$
$$\frac{\partial^2 w}{\partial t^2} = \frac{a}{x^n} \frac{\partial}{\partial x} \left(x^n \frac{\partial w}{\partial x} \right) + w f(u^2 - w^2) + u g(u^2 - w^2).$$

1°. Solution:

$$u = r(x) \cosh[\theta(x) + C_1 t + C_2], \quad w = r(x) \sinh[\theta(x) + C_1 t + C_2],$$

where C_1 and C_2 are arbitrary constants, and the functions $r = r(x)$ and $\theta(x)$ are determined by the system of ordinary differential equations

$$ar''_{xx} + ar'(\theta'_x)^2 + \frac{an}{x} r'_x - C_1^2 r + r f(r^2) = 0,$$
$$ar\theta''_{xx} + 2ar'_x \theta'_x + \frac{an}{x} r\theta'_x + r g(r^2) = 0.$$

2°. For $n = 0$, there is an exact solution of the form

$$u = r(z) \cosh[\theta(z) + C_1 t + C_2], \quad w = r(z) \sinh[\theta(z) + C_1 t + C_2], \quad z = kx - \lambda t.$$